SEARCHING FOR MOTIVATION: NEW PHYSICS AND THE HUBBLE TENSION

Fabrizio Rompineve, Tufts University

based on: 2006.13959, with M. Gonzalez and M. Hertzberg

2004.05049, with G. Ballesteros and A. Notari

New England Theoretical Cosmology, Gravity and Fields Workshop,

July 21, 2020

OUTLINE

• The Hubble tension

decaying Ultra-Light Scalars (dULS)

Beyond GR

Conclusions

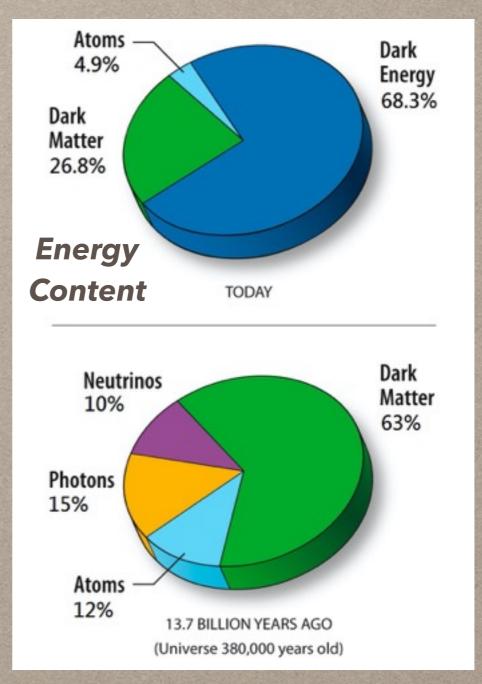
LAMBDA-CDM UNIVERSE

Flat and expanding

$$ds^2 = dt^2 - a(t)^2 d\mathbf{x}^2$$

Effective picture is simple!

Fundamentally, we still don't understand 95% of what is around us!



nasa

THE HUBBLE PARAMETER

Expansion rate

$$H(t) \equiv \frac{\dot{a}}{a}$$
 $H_0 \equiv H(\text{today})$

Measurement



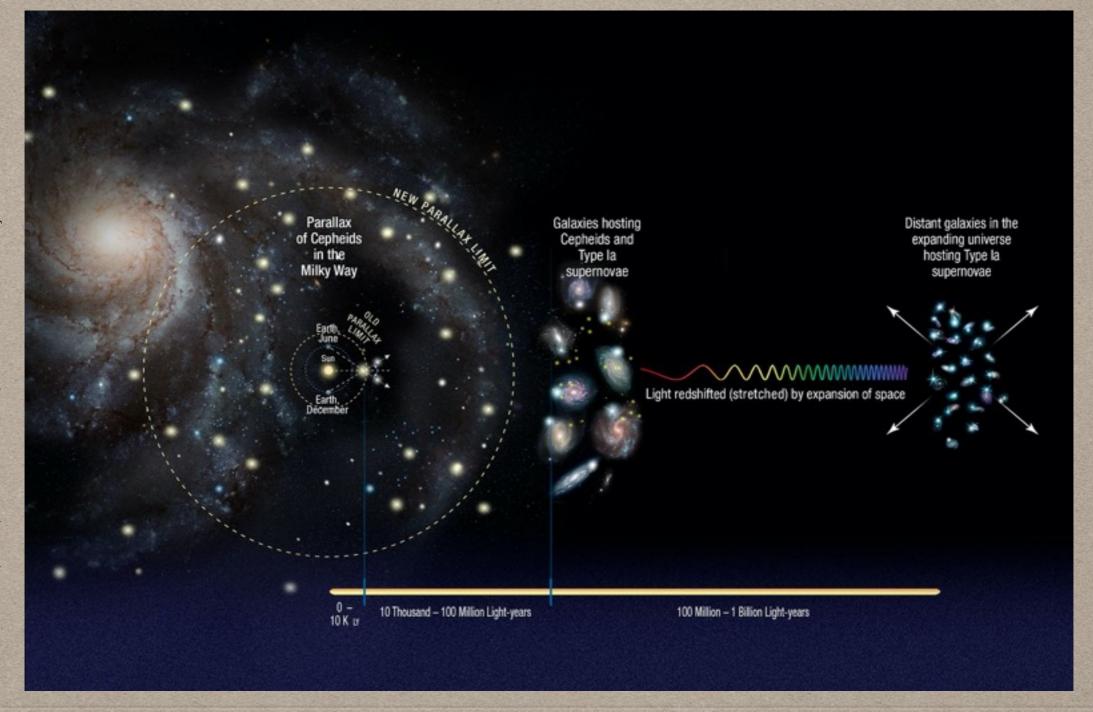
$$z \lesssim 1$$

model-independent

Early Time

 $z \sim 1000$

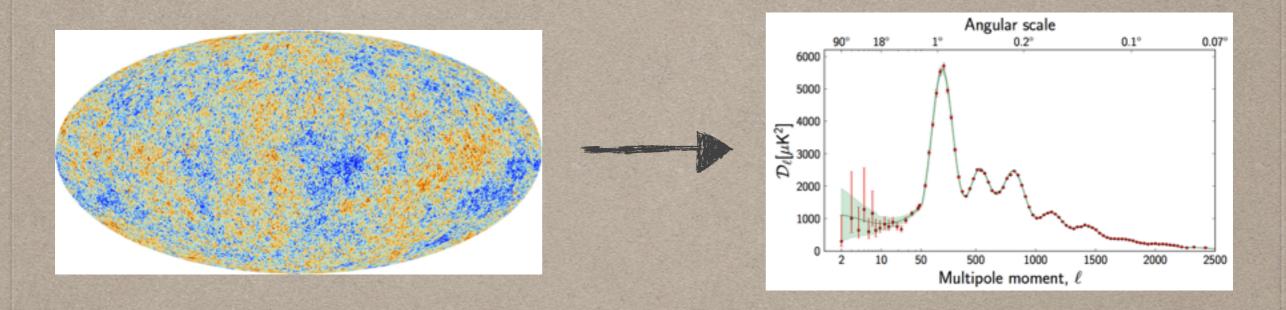
model-dependent



The distance ladder method

Measure redshift z and angular distance D \longrightarrow Get H_0

THE CMB



The shape of the CMB power spectrum is sensitive to variations of cosmological parameters

By performing a **fit** of a **given model** prediction to CMB data, one infers the values of parameters, including H_0

for details, see Knox, Millea 19

THE HUBBLE TENSION

Tension between Planck '18 and SH0ES '19

 4.4σ

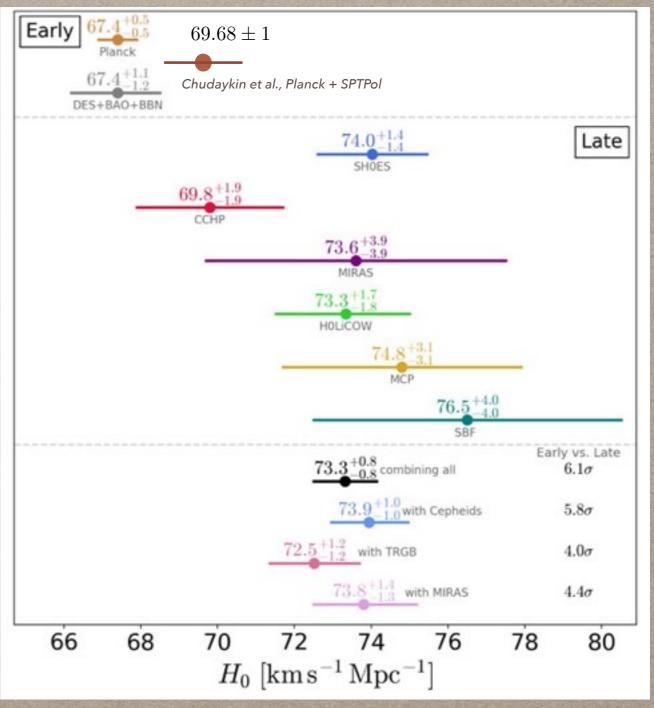
Riess, Casertano, Yuan, Macri, Scolnic 19

Other late measurements tend to agree with SH0ES, but **exceptions exist!**

Until now, **systematics** claimed to be under control.

Motivates search for different cosmological model!

Assuming Lambda-CDM



adapted from Verde, Treu, Riess '19

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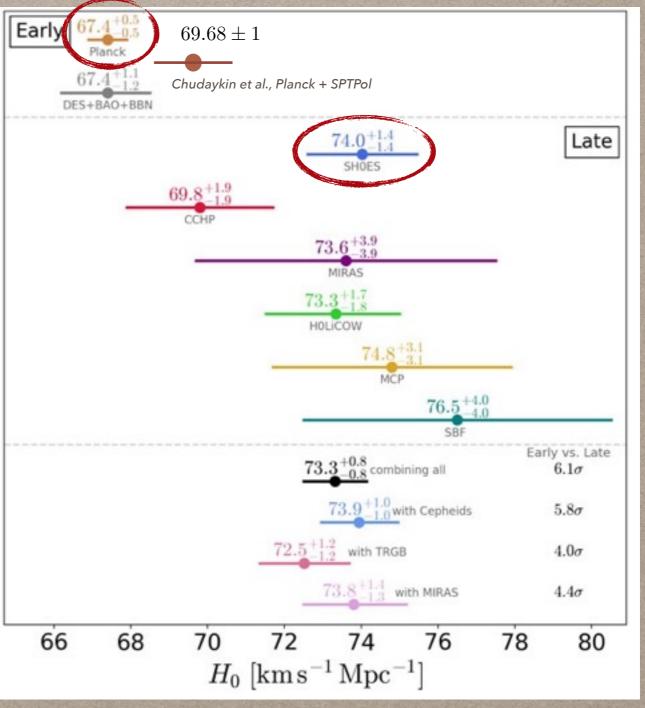
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Extra component should decay at least as fast as radiation not to spoil fit to CMB

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Dark radiation

 $\Delta N_{\rm eff} = N_{\rm eff} - 3.046$



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(Pseudo)scalar fields

with suitable potential which switches on around equality

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coincidence problem!

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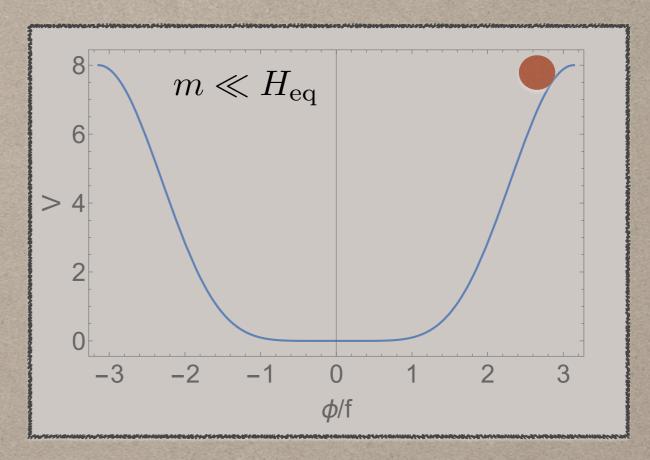
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$$V = m^2 F^2 \left[1 - \cos\left(\frac{\phi}{F}\right) \right]^n$$

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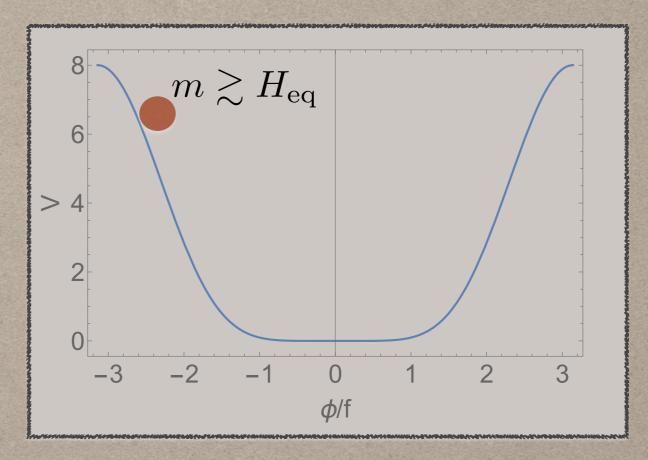
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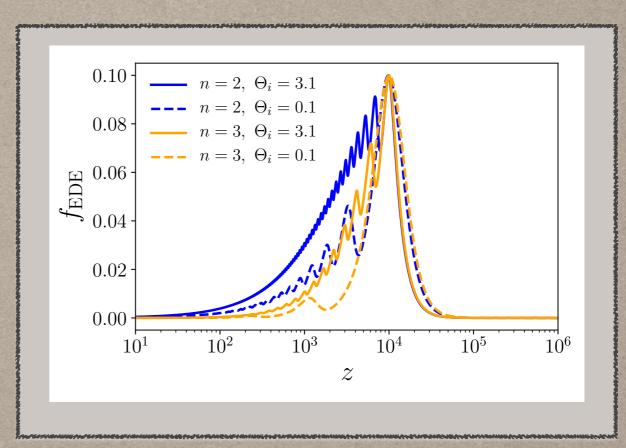
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$$m \sim H_{\rm eq}, F \sim 0.1 M_p$$

provides best-fit to
Planck+BAO+Pantheon+SH0ES



Smith, Poulin, Amin 19

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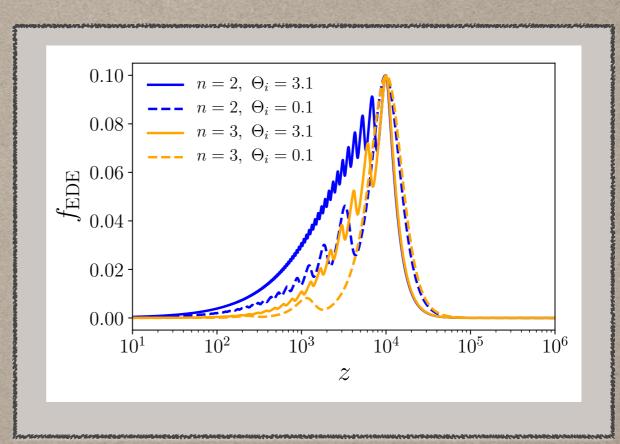
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Smith, Poulin, Amin 19

Caveat: Large Scale Structure (LSS) data constrains improvement over Lambda-CDM!

see talk by Evan later today!

 S_8 tension'

Poulin, Smith, Karwal, Kamionkowski 18 Agrawal, Cyr-Racine, Pinner, Randall 19 Hill, McDonough, Toomey, Alexander 20 Recent addition of BOSS full-shape

Ivanov, McDonough, Hill, Simonovic, Toomey, Alexander, Zaldarriaga 20 D'Amico, Senatore, Zhang, Zheng 20

SEARCHING FOR MOTIVATION

In this talk instead: model-building perspective

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Can better-motivated models convincingly address the tension?

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EDE POTENTIAL

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 $c_2/c_1 = -2/5, c_3/c_1 = 1/15$ $c_{i>3} = 0$

Poulin, Smith, Karwal, Kamionkowski 18

conspiracy among harmonics hides severe tuning!

2006.13959, with M. Gonzalez and M. Hertzberg

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Here instead we want to keep the standard axion potential

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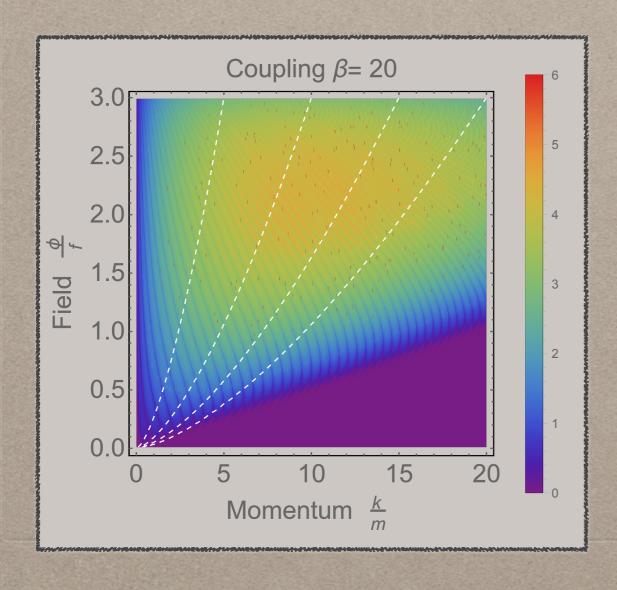
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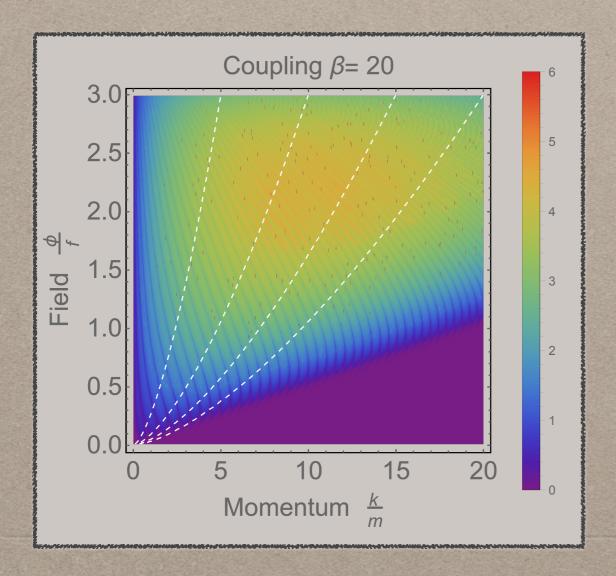
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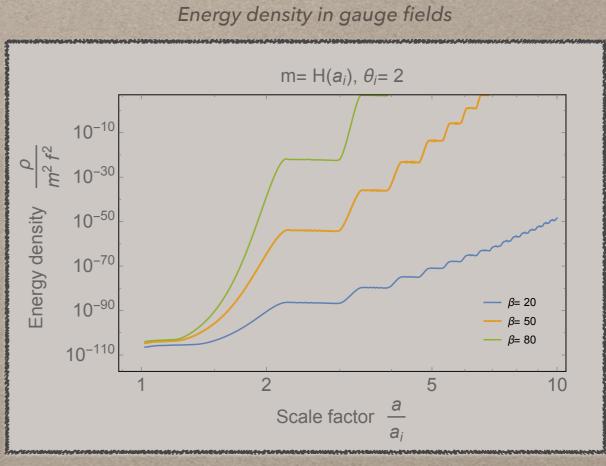
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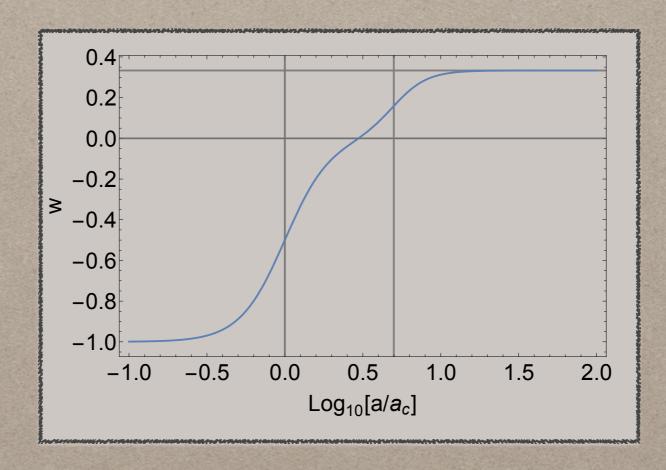
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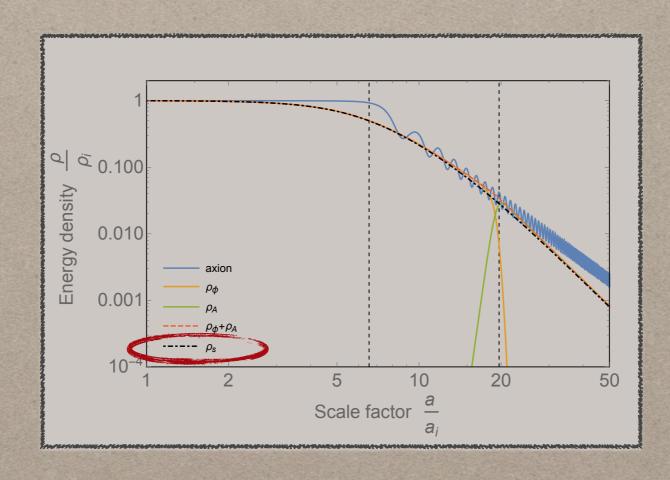
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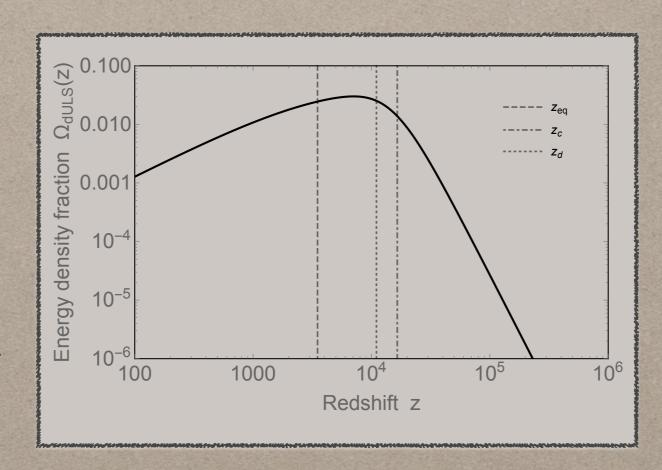


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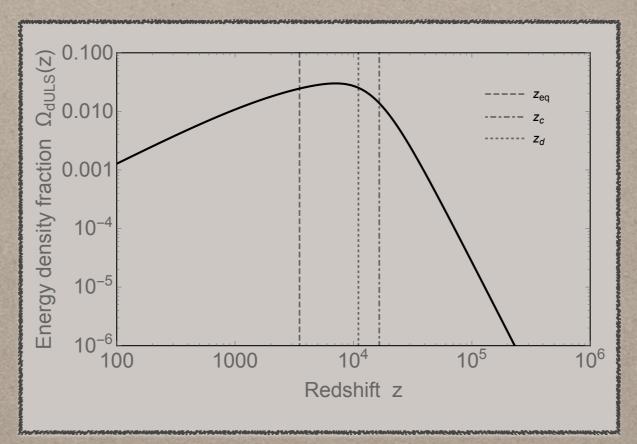
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see also Poulin et al 18, Lin et al 19

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Treatment of perturbations is more subtle.

We used a simplified picture with sound speed tracking the equation of state parameter

RESULTS

Dataset: Planck 18 + BAO + Pantheon + SH0ES 19

Parameter	ACDM	dULS	$\Delta N_{ m eff}$
$100 \omega_b$	$2.254 (2.26)^{+0.013}_{-0.014}$	$2.261 (2.249)^{+0.019}_{-0.019}$	$2.272 (2.268) \pm 0.017$
$\omega_{ m cdm}$	$0.1183 \ (0.1189)^{+0.00087}_{-0.00092}$	$0.1232 \ (0.124)^{+0.0023}_{-0.0024}$	$0.1235 (0.123)_{\pm} 0.0029$
$10^9 A_s$	$2.122 (2.123)_{-0.035}^{+0.03}$	$2.138 (2.143)^{+0.035}_{-0.04}$	$2.147 (2.135)^{+0.033}_{-0.036}$
$ n_s $	$0.97 (0.9699)^{+0.0038}_{-0.0036}$	$0.9812 \ (0.9822)^{+0.0079}_{-0.0085}$	$0.9793 (0.98) \pm 0.0062$
$ au_{ m reio}$	$0.06053 (0.06027)_{-0.0084}^{+0.007}$	$0.06042 (0.05883)^{+0.0079}_{-0.0086}$	$0.0604 (0.05753)^{+0.0072}_{-0.0081}$
H_0	$68.24 \ (68.06) \pm 0.41$	$69.69 (69.67)_{-0.83}^{+0.81}$	$69.96 (69.82)_{-1}^{+0.98}$
$10^6 \Omega_{\rm dULS}/\Delta N_{\rm eff}$	_	$7.387 (9.021)_{-3}^{+2.9}$	$0.3107 (0.2865)^{+0.16}_{-0.17}$
$10^5 a_c$	-	$4.526 (6.053)_{-2.5}^{+2.4}$	_
g_d	_	fixed to 1.5	-
σ_8	$0.8097 (0.8119)^{+0.0061}_{-0.0067}$	$0.8231 \ (0.8251)^{+0.0094}_{-0.01}$	$0.8245 \ (0.8215) \pm 0.01$
$\Delta \chi^2$	0	-7.92	-2.78

Table I. The mean (best-fit in parenthesis) $\pm 1\sigma$ error of the cosmological parameters obtained by fitting Λ CDM, the dULS and the $\Delta N_{\rm eff}$ models to our combined cosmological dataset.

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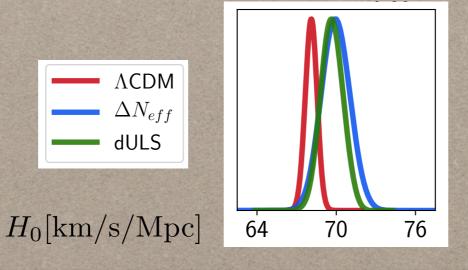
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Very similar to dark radiation, but significantly improved χ^2

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Take home:

Scenarios of **EDE/dULS**do not **convincingly** address
the Hubble tension.

A DIFFERENT ATTEMPT: BEYOND GR 2004.05049

EDE/dULS models feature a coincidence problem: why should a dynamical transition occur at equality?

A simple theory where such a transition occurs naturally around equality is that of a non-minimally coupled scalar

$$S = \frac{1}{2} \int d^4x \sqrt{-g} \left[M^2 f(\phi) R + \partial_{\mu} \phi \partial^{\mu} \phi + L_{\text{tot}} \right]$$

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$$f(\phi) = 1 + \beta \left(\frac{\phi}{M} \right)^2$$
 with $\beta < 0$

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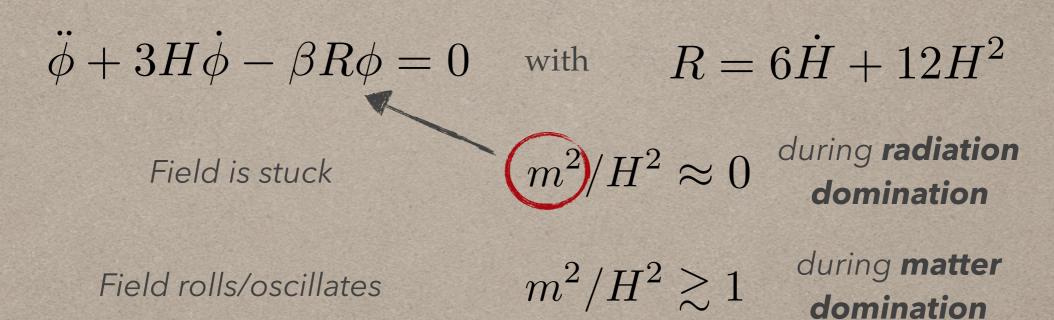
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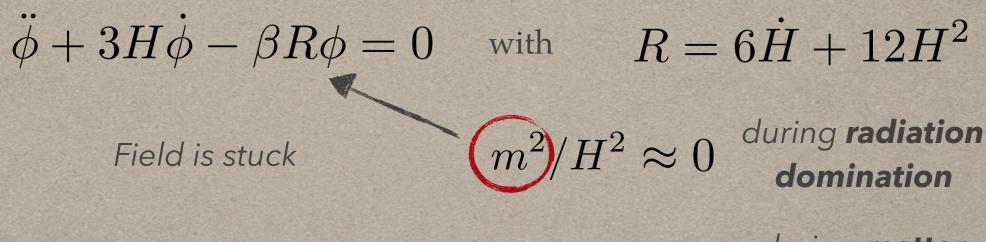
related ideas

$$S = \frac{1}{2} \int d^4x \sqrt{-g} \left[M^2 f(\phi) R + \partial_\mu \phi \partial^\mu \phi + L_{\rm tot} \right]$$
 e.g.
$$f(\phi) = 1 + \beta \left(\frac{\phi}{M} \right)^2$$
 Variation of Newton constant from early time to today
$$\Delta G_{\rm N} \approx \beta \phi^2$$
 see also Lin et al. 18/Rossi et al/Solá et al/Sakstein et al. 19/Zumalacarregui 20/... for

$$\ddot{\phi} + 3H\dot{\phi} - \beta R\phi = 0 \quad \text{with} \quad R = 6\dot{H} + 12H^2$$

$$\ddot{\phi}+3H\dot{\phi}-\beta R\phi=0$$
 with $R=6\dot{H}+12H^2$ Field is stuck
$$m^2/H^2\approx 0 \ \ {\rm during\ radiation\ domination}$$

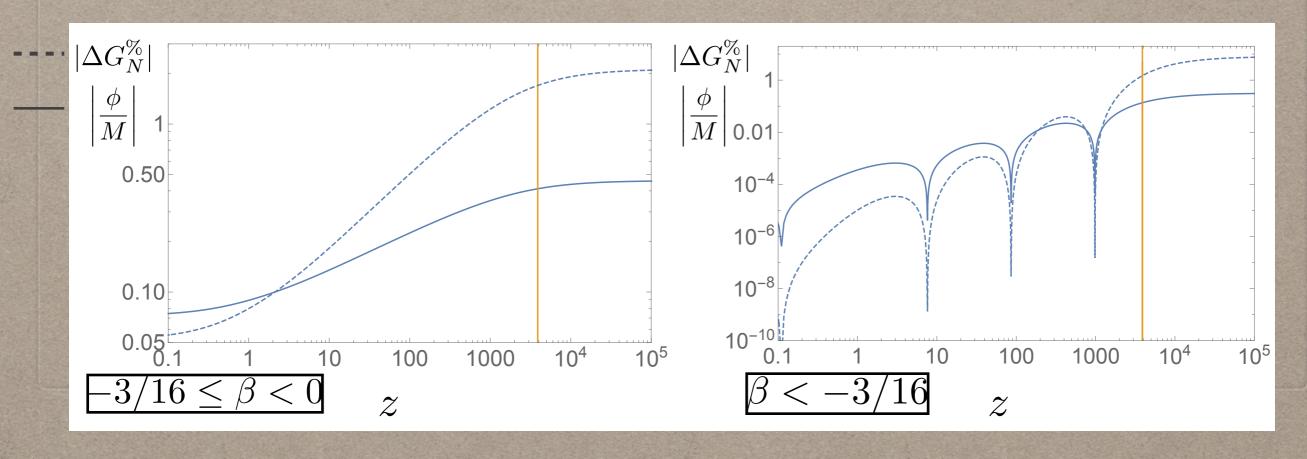


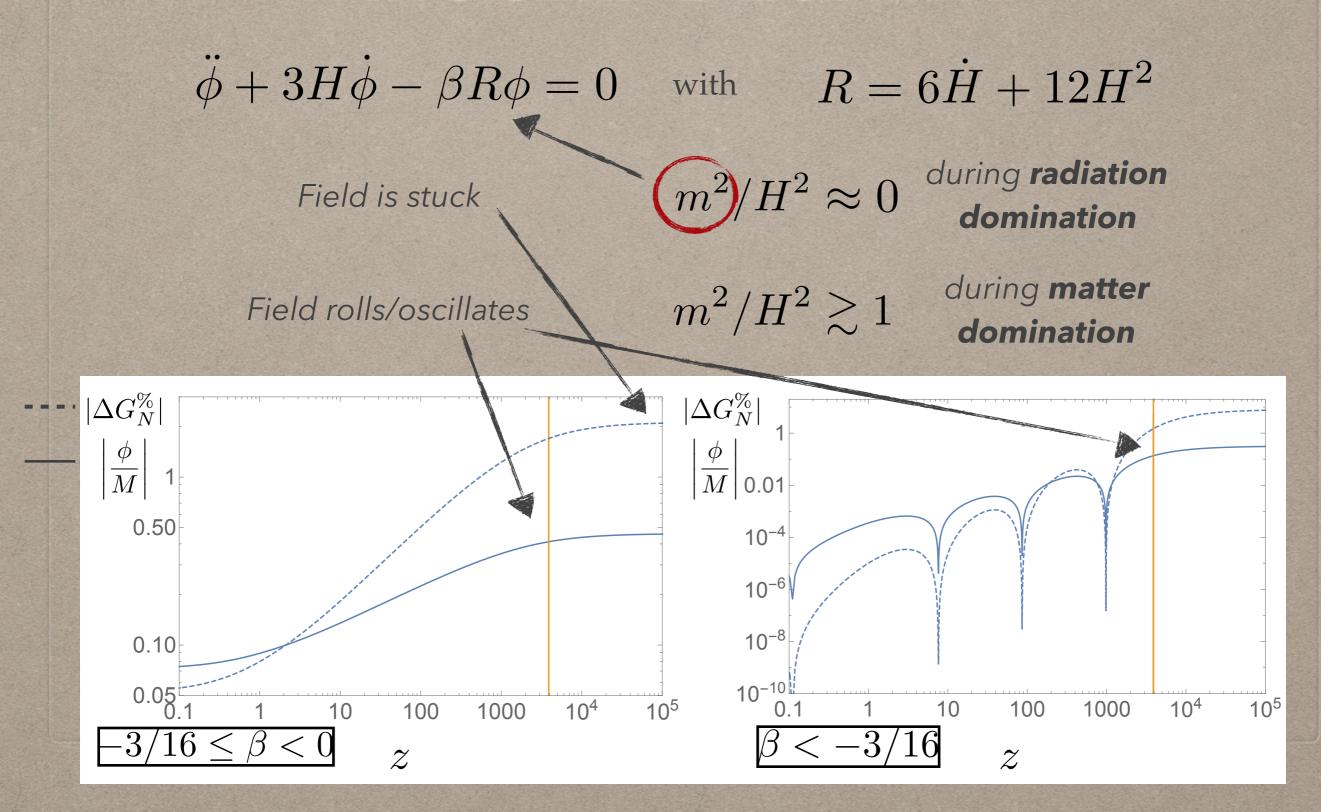


Field rolls/oscillates

$$m^2/H^2 \gtrsim 1$$

during matter domination





DISCUSSION

Fit to CMB gives results similar to dark radiation when neglecting post-newtonian constraints (screening mechanisms? late time dynamics of the field?)

see 2004.05049 for details

Constraints from LSS?

CONCLUSIONS

- Hubble tension may hint at additional complexity beyond Lambda-CDM.
- Early Dark Energy (EDE) models require tuned UV setups.
- decaying ultralight scalar (dULS) models are well-behaved
 EFTs, but UV realization requires additional ingredients!

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- Non-minimally coupled scalars explain why dynamical transition occurs around equality!
- However, tension is only alleviated in simple models.

THE SEARCH CONTINUES



Thank you for the attention!

BACKUP

RESONANT DECAY

$$\ddot{\phi} + 3H\dot{\phi} + V'(\phi) = 0$$

caveat: neglect back reaction!

$$\ddot{\mathbf{A}} + H\dot{\mathbf{A}} - \frac{\nabla^2}{a^2}\mathbf{A} + \frac{\beta}{f}\dot{\phi}\frac{\nabla}{a} \times \mathbf{A} = 0$$

see Kitajima, Sekiguchi, Takahashi 17

in Fourier space

$$\ddot{s}_{\mathbf{k},\pm} + H\dot{s}_{\mathbf{k},\pm} + \left[\left(\frac{k}{a} \right)^2 \mp \frac{k}{a} \frac{\beta}{f} \dot{\phi} \right] s_{\mathbf{k},\pm} = 0$$

Tachyonic resonance

Effective frequency

$$\omega_k^2 \equiv k(k \mp \beta/f\dot{\phi})$$

can go negative

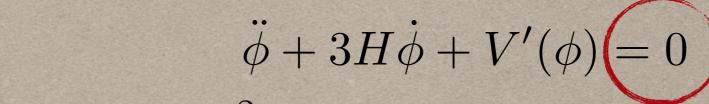
Parametric resonance

see Floquet bands where

$$s_{\mathbf{k},\pm} \sim e^{\mu_k t} P(t)$$

$$\mu_k > 0$$

RESONANT DECAY



caveat: neglect back reaction!

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RESONANT DECAY

Energy in the gauge fields

$$\rho_A = \frac{1}{2a^4} \int \frac{d^3k}{(2\pi)^3} \sum_{\pm} \left(a^2 |\dot{s}_{\pm}|^2 + k^2 |s_{\pm}|^2 - 2k \right)$$

SCALAR RESONANT DECAY

$$\mathcal{L} = \frac{1}{2}(\partial\phi)^2 + \frac{1}{2}(\partial\chi)^2 - \frac{1}{2}m^2\phi^2 - \frac{1}{2}\epsilon\phi\chi^2$$

Efficient resonant decay for
$$\epsilon\gg \frac{m^2}{\phi_i}$$
 fine, since $m\ll f$

SCALAR RESONANT DECAY

$$\mathcal{L} = \frac{1}{2}(\partial\phi)^2 + \frac{1}{2}(\partial\chi)^2 - \frac{1}{2}m^2\phi^2\left(-\frac{1}{2}\epsilon\phi\chi^2\right)$$

Efficient resonant decay for $\left(\epsilon\gg rac{m^2}{\phi_i}
ight)$ fine, since $\ m\ll f$

However, how to justify lightness of χ ?

$$\mathcal{L}_{UV} = |\partial \Phi|^2 - \lambda(|\Phi|^2 - v^2)^2$$

with
$$\Phi = v + (\phi + i\chi)/\sqrt{2}$$

then
$$m=\sqrt{2\lambda}v, \quad \epsilon=2\lambda v$$

and condition above requires $|\phi_i|\gg v$

SCALAR RESONANT DECAY

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and condition above requires $|\phi_i|\gg v$ standard resonance analysis does not apply!

NON-MINIMALLY COUPLED SCALAR

When writing Friedmann equation as

$$3H^2M^2 = \rho_{\phi} + \rho_{\text{tot}}$$

one finds

$$\rho_{\phi} = \frac{1}{2}\dot{\phi}^2 - 6\beta H\dot{\phi}\phi - 3\beta H^2\phi^2$$

When writing Friedmann equation as

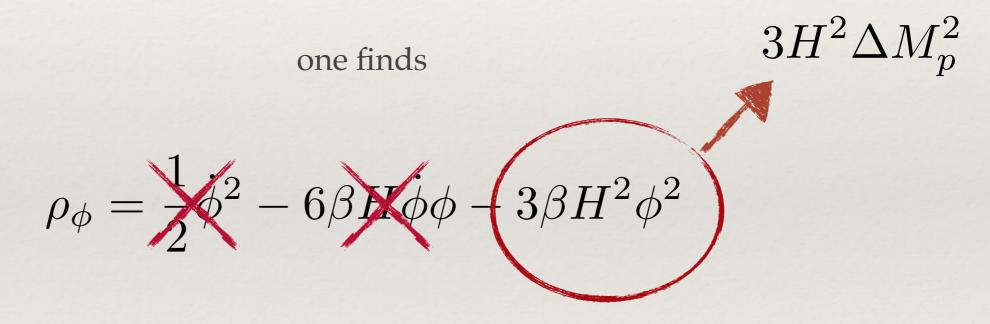
$$3H^2M^2 = \rho_\phi + \rho_{\rm tot}$$

one finds
$$3H^2\Delta M_p^2$$

$$\rho_\phi = \frac{1}{2}\dot{\phi}^2 - 6\beta H\dot{\phi}\phi + 3\beta H^2\phi^2$$

When writing Friedmann equation as

$$3H^2M^2 = \rho_{\phi} + \rho_{\text{tot}}$$



Before equality

$$\rho_{\phi} \sim H^2 \sim a^{-4}$$

When writing Friedmann equation as

$$3H^2M^2 = \rho_\phi + \rho_{\rm tot}$$

one finds

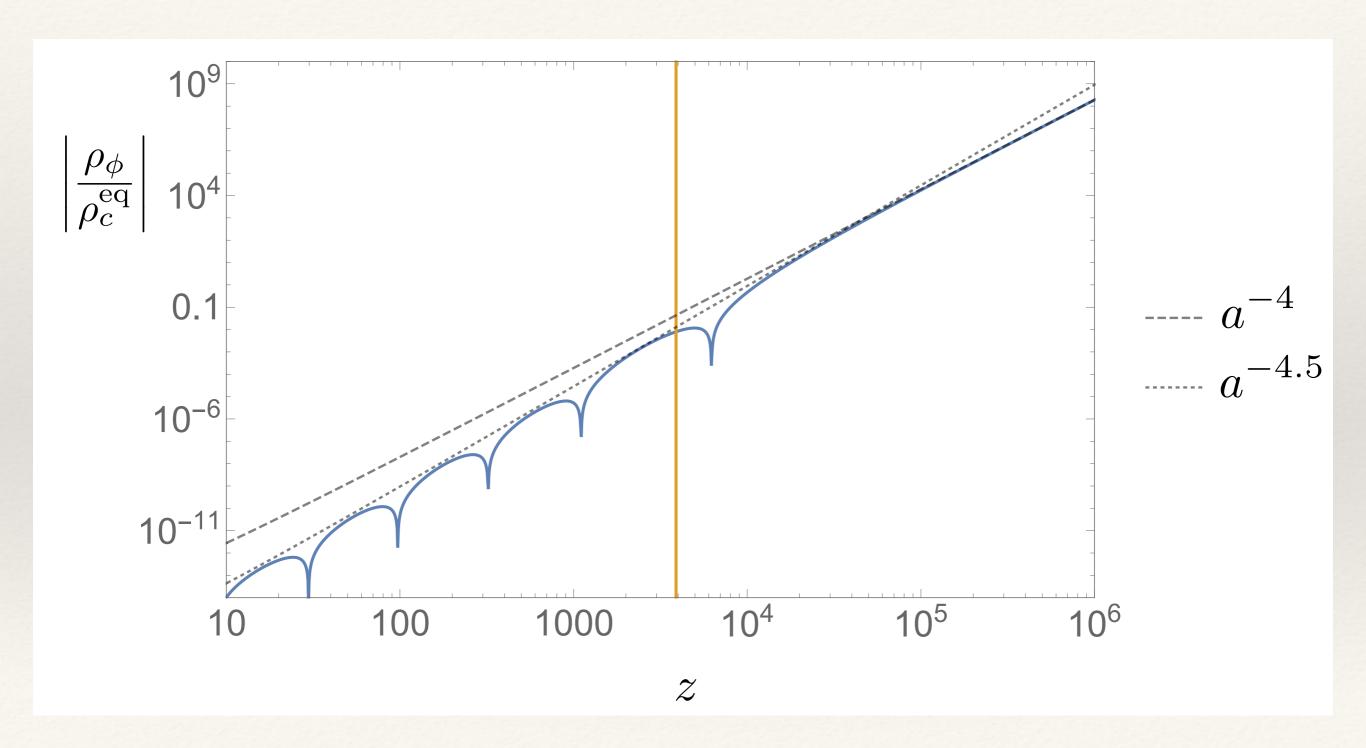
$$\rho = \frac{1}{2}\dot{\phi}^2 - 6\beta H\dot{\phi}\phi - 3\beta H^2\phi^2$$

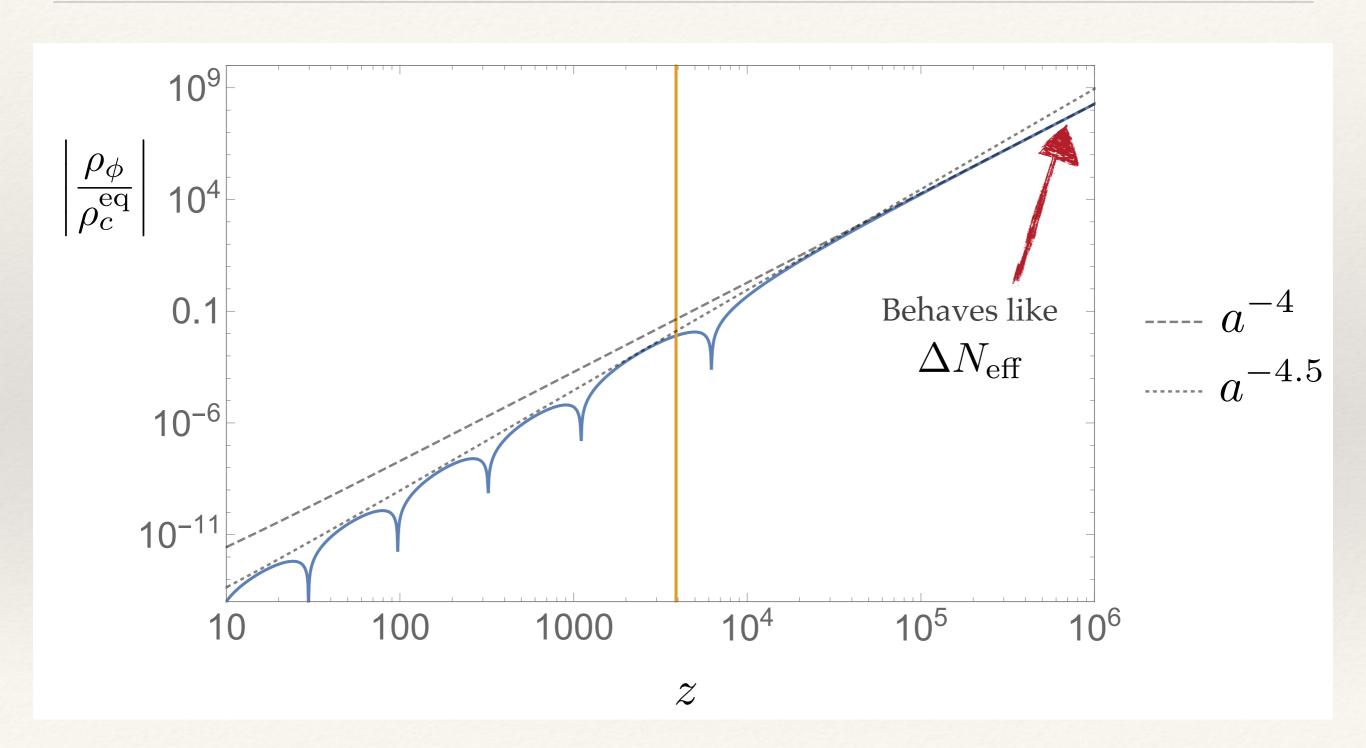
Before equality

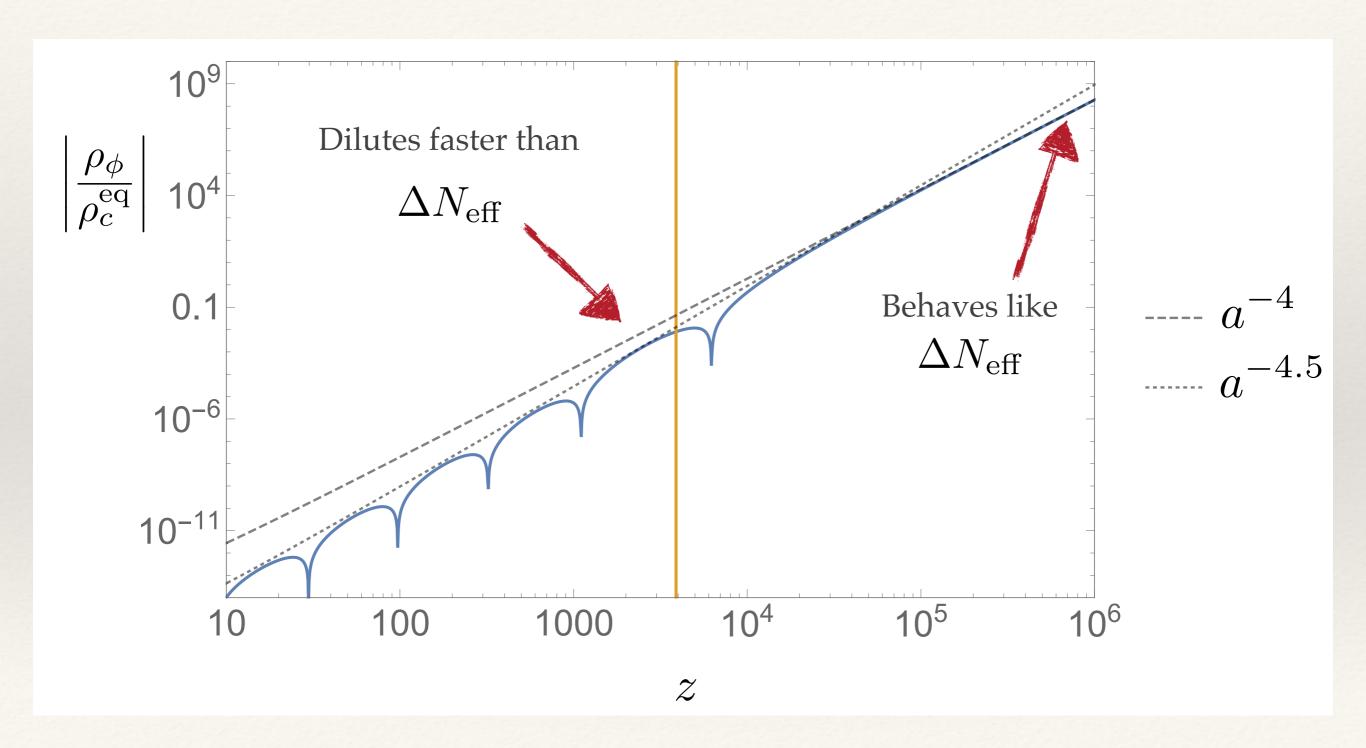
After equality

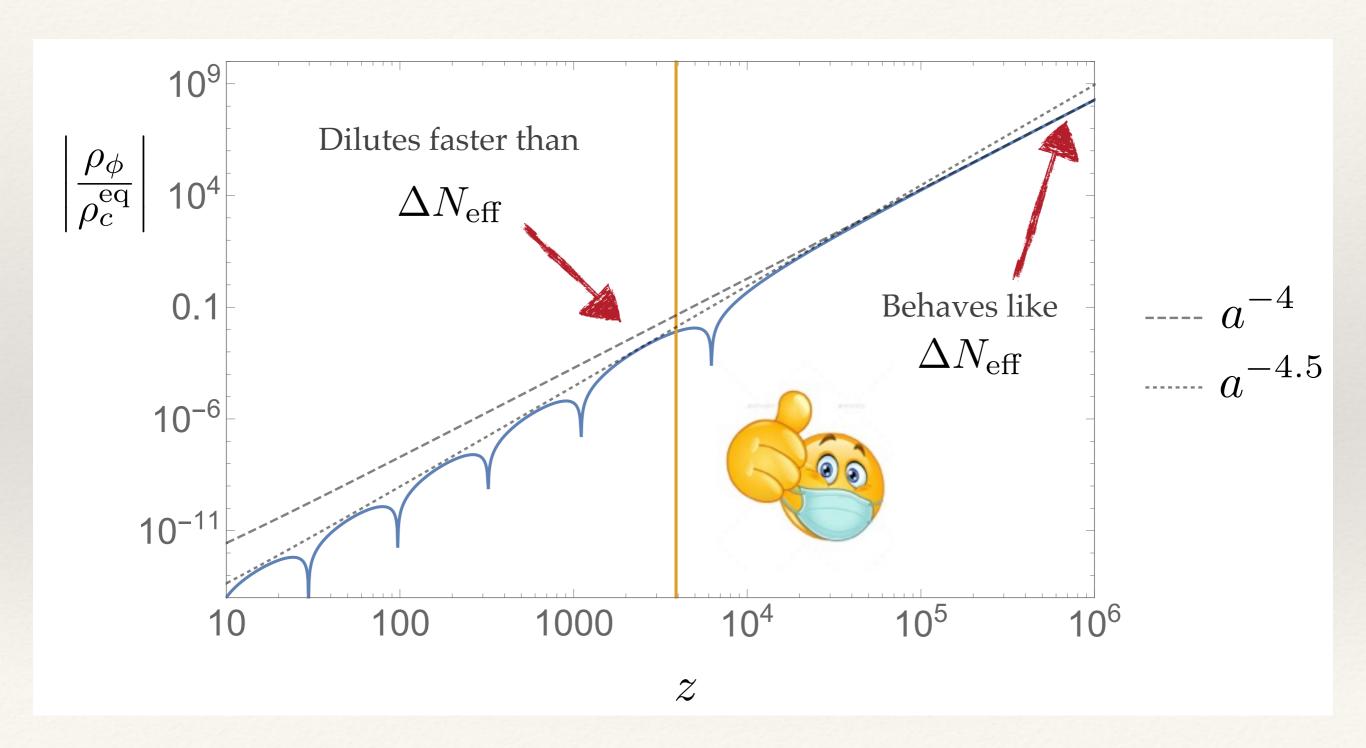
$$\rho_{\phi} \sim H^2 \sim a^{-4}$$

$$\rho_{\phi} \sim a^{-9/2}$$

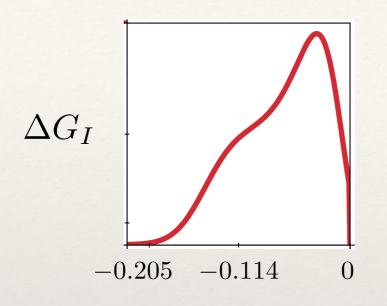


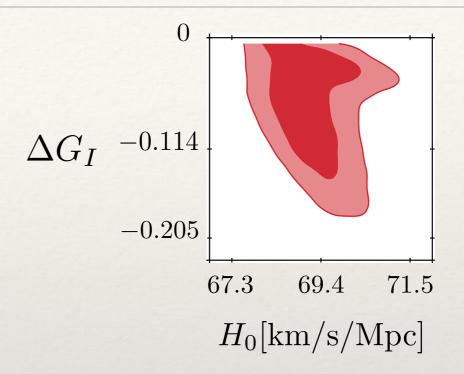


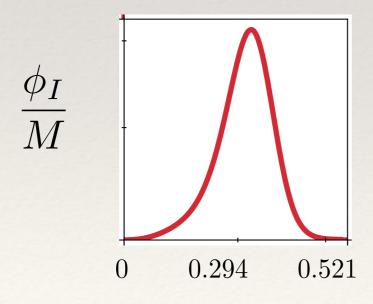


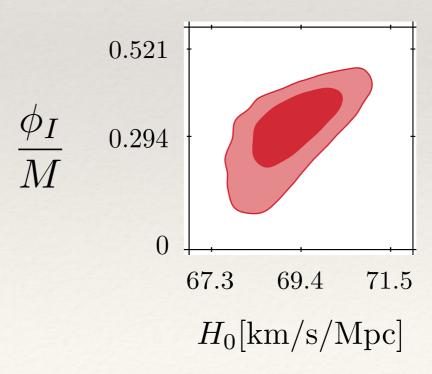


Results

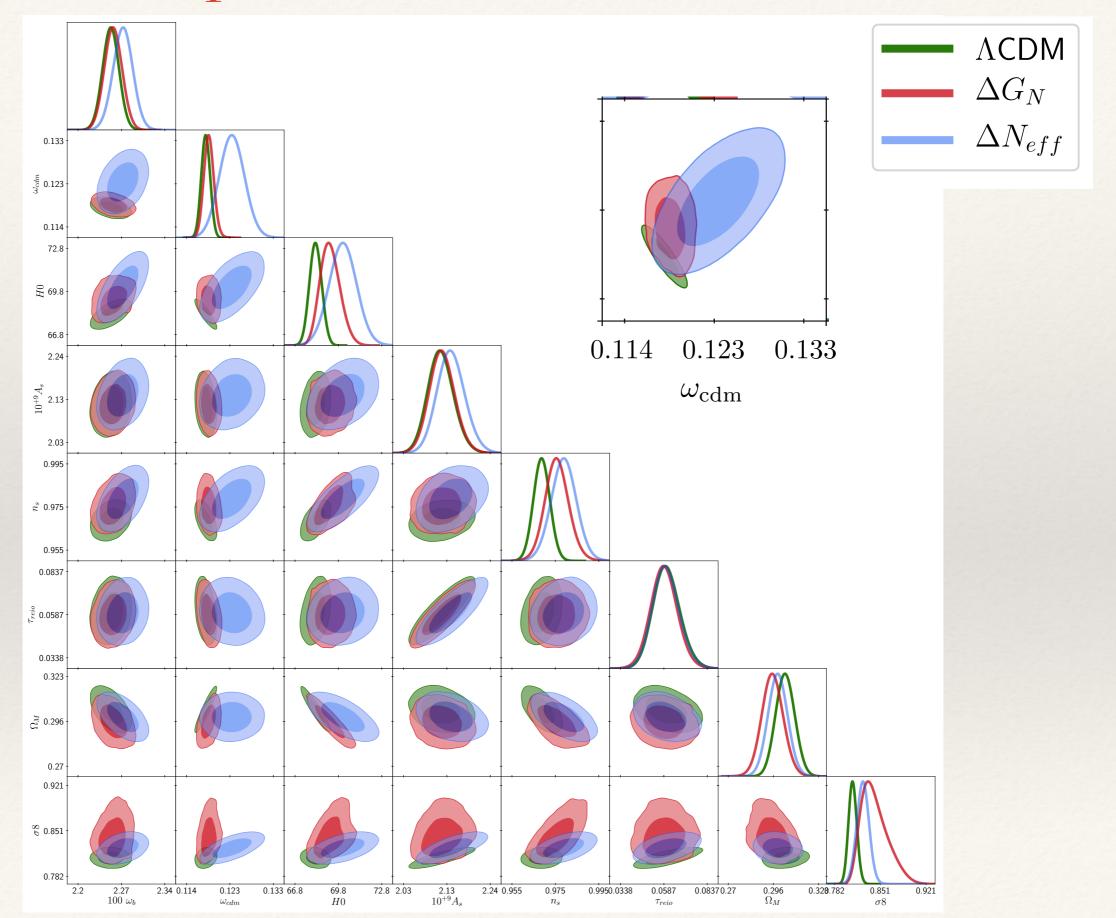








Comparison with Dark Radiation



Comparison with Dark Radiation

