

# Core Loss Initiative: Technical

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THAYER SCHOOL OF  
ENGINEERING  
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## Saturday workshop summary

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- Morning topic: **Core loss**
- Afternoon topic: **Fringing**
- My impossible task: **Summarize both sessions.**



# Core loss



- Behaviors to capture in models, measurements and data sheets.
  - Nonlinearity
  - Different behavior at different frequencies.
  - Effect of complex waveforms.
  - Impact of physical dimensions.**
- Measurement Accuracy Issues (Stefan Ehrlich, Fraunhofer Institute)
  - Precision needed and how to achieve it.

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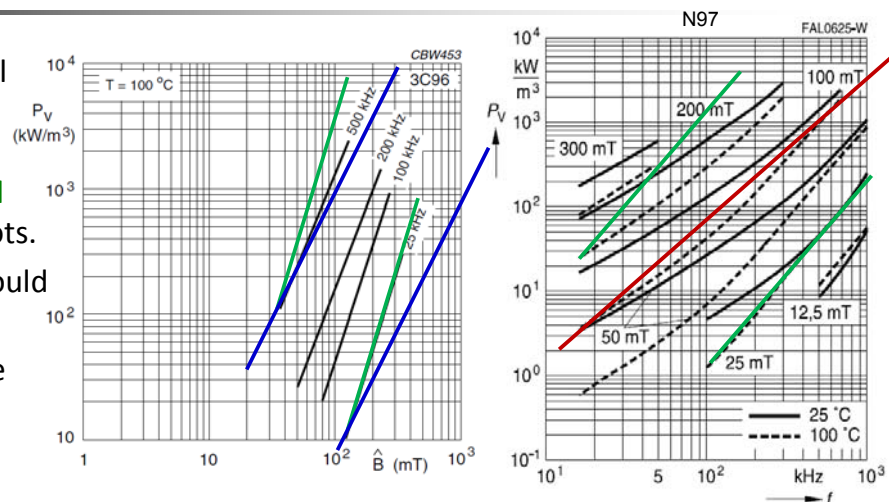


# Nonlinearity and frequency dependence



- Steinmetz model  

$$P = kf^\alpha \hat{B}^\beta$$
 would mean  
**straight, parallel**  
 lines on both plots.
- Linear** model would mean  $\beta = 2$ .
- Behavior is more complex.



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## How to capture nonlinear frequency dependent loss data?



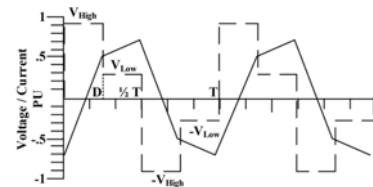
- Just collect the data and interpolate.
- Better curve fits.
  - Example:  $P = k_1 \cdot f^\alpha \cdot B^\beta + k_2 \cdot f^\gamma \cdot B^\zeta$
- Dynamic models that inherently have the right dependence on  $f$  and  $B$ .
  - Example of a first attempt at this from Ray Ridley—work in progress.

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## Omitted in all of the above



Issue	Implication
DC bias effect	Data collection needed
Variety of waveforms	Options include <ul style="list-style-type: none"> <li>• Extrapolation from limited data (e.g., iGSE method)</li> <li>• Comprehensive “loss map” data collection for waveforms of interest.               <ul style="list-style-type: none"> <li>• e.g., Byron Beddingfield’s DAB tester for “dual slope” waveforms.</li> </ul> </li> </ul>
Effect of core size and shape	Effects to study: <ul style="list-style-type: none"> <li>• Skin effect</li> <li>• Wave propagation/dimensional resonance</li> <li>• Mechanical resonance</li> <li>• Simple flux crowding as affected by shape</li> </ul>

*Last year's talk—slides at URL below*

*Discussed next*

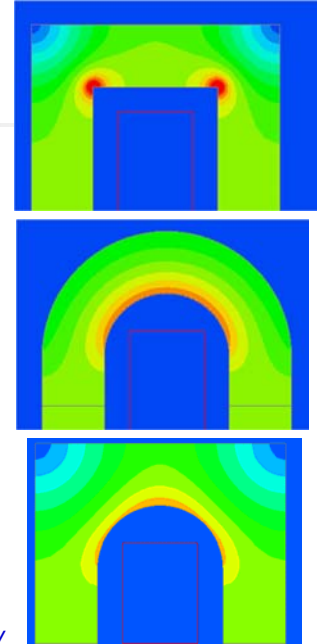
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## Dimensional Effects

- Straightforward to model and analyze:
  - Flux crowding at corners.
  - Cross section variation.
  - See blog post for more on examples at right.
- Complex, known physics; uncertain parameters:
  - Skin effect and wave propagation
  - Mechanical vibration: [See ref \[5\]\\*](#).
- Poorly understood:
  - Higher loss on surfaces than in bulk.



*\*Slides in on the memory stick are only a placeholder. Find these, with references, at [sites.dartmouth.edu/power-magnetics/](http://sites.dartmouth.edu/power-magnetics/)*

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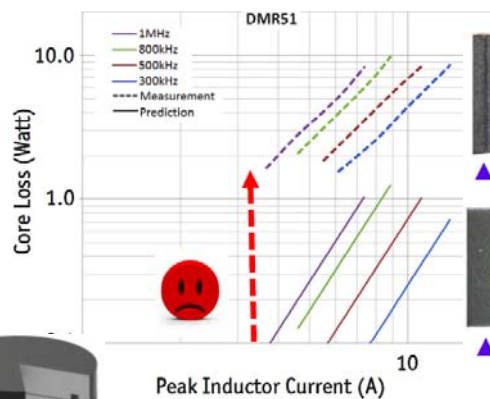


## Surface losses in MnZn ferrite confirmed



- Confirmed to be surface effect by dynamic calorimetry.  
D. Neumayr, D. Bortis, J. W. Kolar, ETH Zurich.
- A prototype with NiZn ferrite does not have this problem.

Talk Wed. 09:45,  
"A Low-Loss Inductor ....",  
Session T12, Magnetics,  
paper 1487, Yang, Hanson,  
Perreault and Sullivan.



▲ Stack Of 1mm Plates



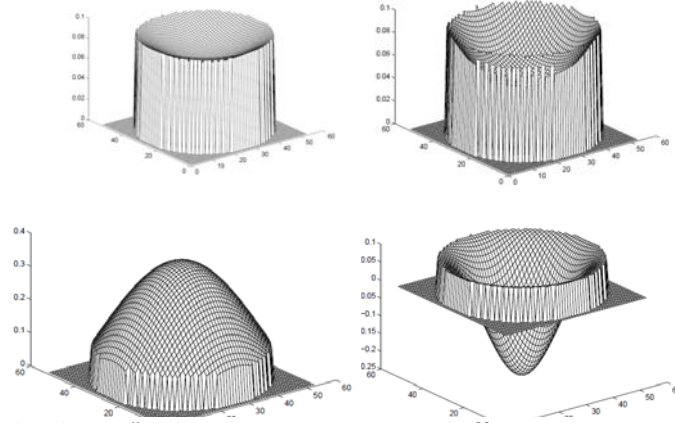
▲ Solid Sample



## Dimensional Effects: plots of $|B|$ in a round centerpost



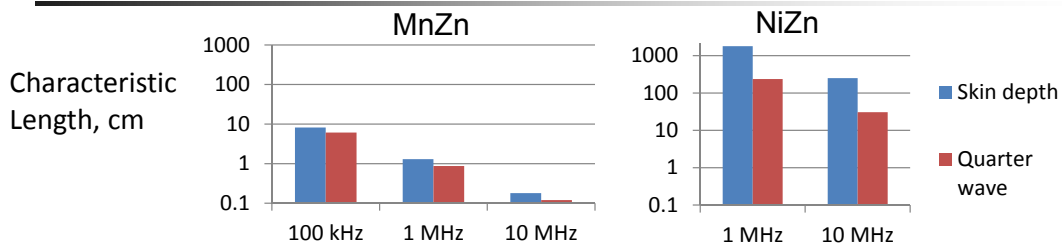
- Skin effect, affected by  $\mu$  and  $\sigma$  (permeability and conductivity)
- Wave propagation (dimensional resonance) affected by  $\mu$  and  $\epsilon$  ( $\epsilon$  = permittivity or dielectric const.)
  - Typ.  $\epsilon_r = 10^5$  for MnZn ferrite



- Figures from Glenn Skutt's excellent PhD thesis: "High-Frequency Dimensional Effects in Ferrite-Core Magnetic Devices," Virginia Tech, 1996.



## Rough core leg size for these effects



- For low loss, skin effect may be important sooner than shown.

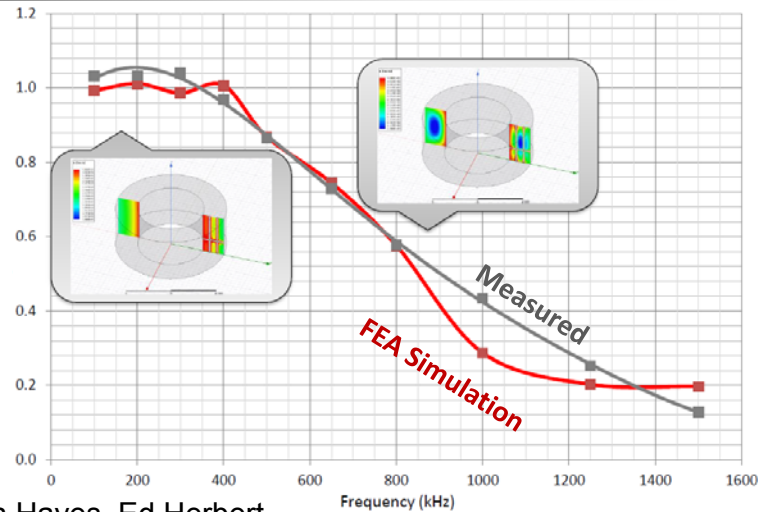


## SMA/PSMA/UCC experiments

Drilled MnZn core to install  
sense windings.



Flux  
ratio:  
A/B  
(inner/  
outer)



Marcin Kacki, Myrek Rylko, John Hayes, Ed Herbert

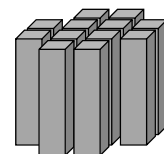
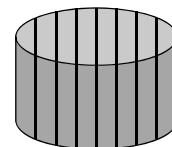
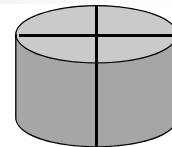
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## Dimensional effects: implications



- For large area core legs at high frequency:
  - Segmented, laminated, or “bundle of sticks” approach.
  - Measurement data taken on a different core size may not be adequate.
- Very rough idea of size and frequency thresholds
  - ~ 1 cm at 1 MHz with MnZn ferrite.
  - ~ 1 cm at 10 MHz with NiZn ferrite.
- Data on  $\epsilon$  and  $\rho$  combined with streamlined modeling could avoid the need for loss measurement of every core size.
- Caution:  $\epsilon$  and  $\rho$  vary with frequency and temperature.

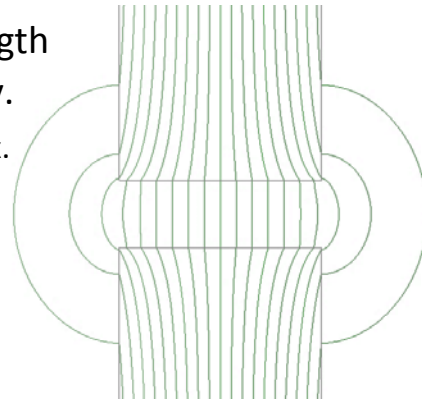




## Afternoon: Fringing



- Changes air-gap reluctance.
  - Calculations rarely needed: design based on reluctance  $\mathcal{R}$ , not gap length  $\ell_g$ , and find the gap experimentally.
  - If needed, calculations are in the appendix.
- Extra winding loss.
- Extra core loss in laminated/tape wound cores: eddy currents.



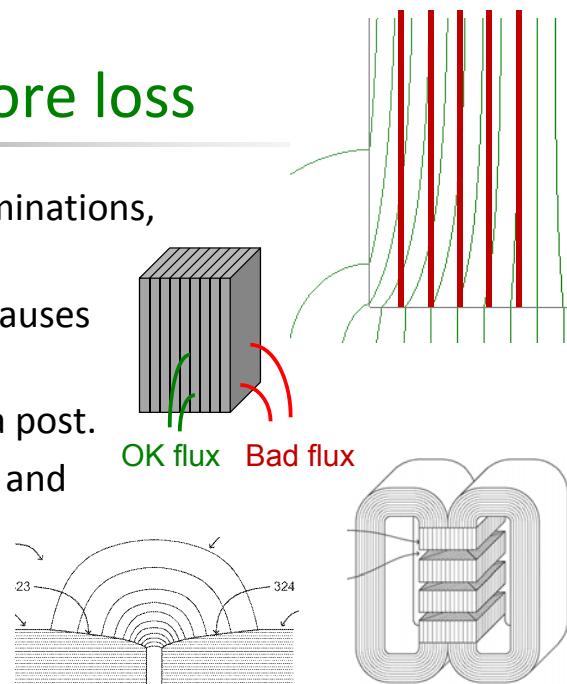
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## Fringing effect on core loss

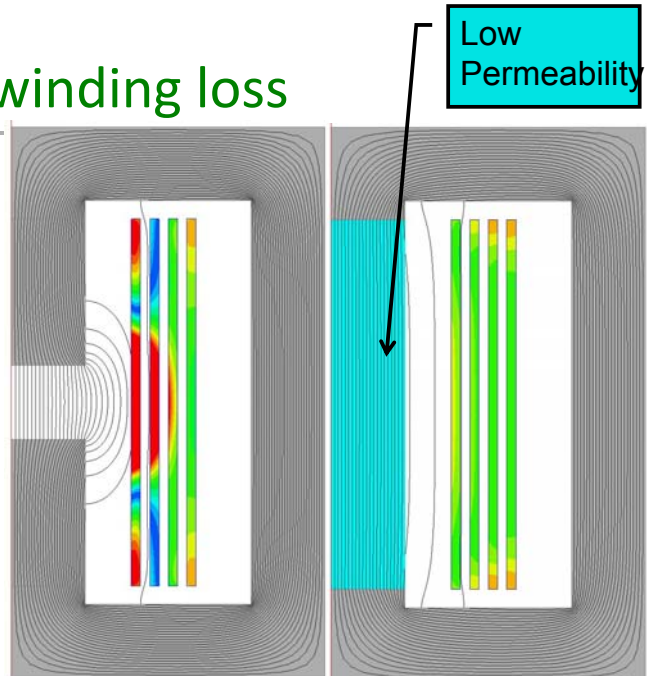
- Flux crosses perpendicular to laminations, inducing loss.
- The “out-of-plane flux” (OOPF) causes excess power loss  $P_{OOPF}$ .
- Only a problem on two sides of a post.
- Solutions exist: patented shapes and configurations [9],[10].





## Fringing effect on winding loss

- Strong field near the gap causes increased eddy-current winding loss.
- Curved field is bad for foil windings:



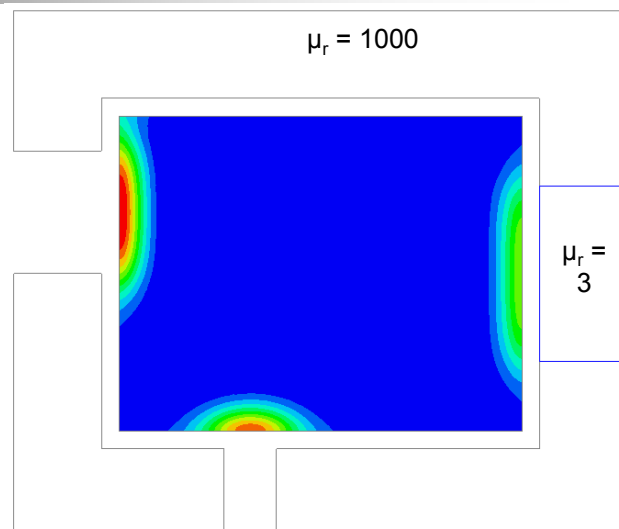
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## One conceptual approach



- Solid winding.
- Current flow is attracted to gaps.
- Amount of current is proportional to gap reluctance.



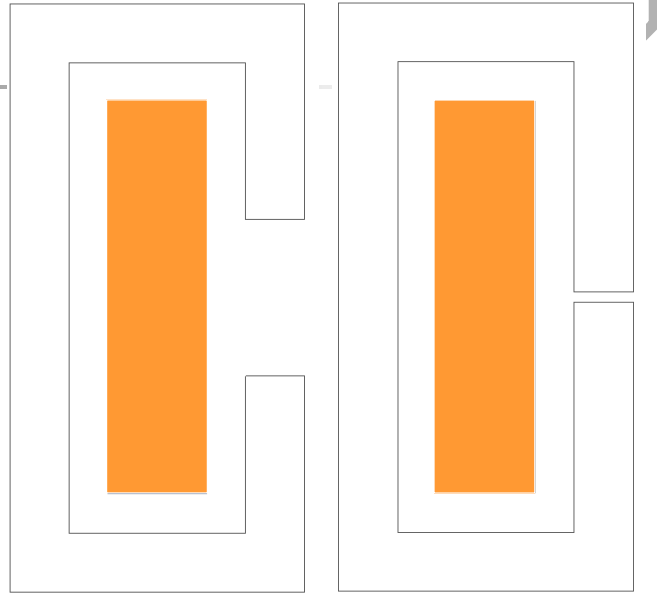
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## Single gap

- Which winding has larger loss, with the same ac current in each winding?



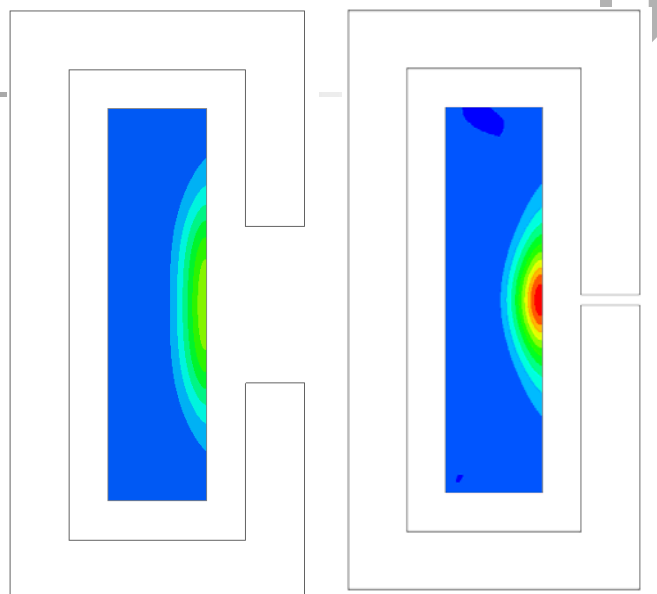
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## Single gap

- All current flows near the gap.
- Longer gap → Current is spread over a larger area → lower loss.
- Current with small gap is spread wider than gap.



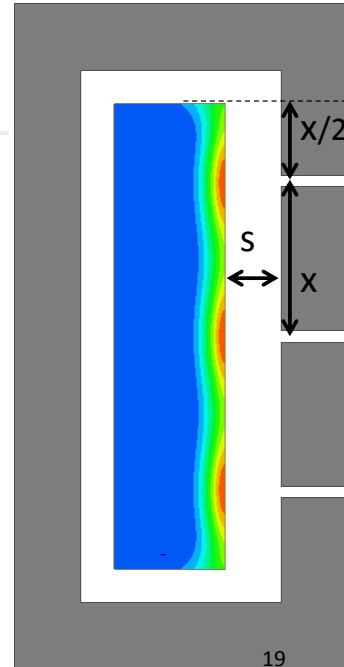
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## One design approach:

- Spread several gaps evenly:
  - Spacing  $x$  between gaps.
  - Distance  $x/2$  from edge of winding.
- Choose spacing  $s < x/3$ .
- Current distribution is not perfect, but “pools” of current overlap and impact on loss is small.
- For details, see ref. [1]

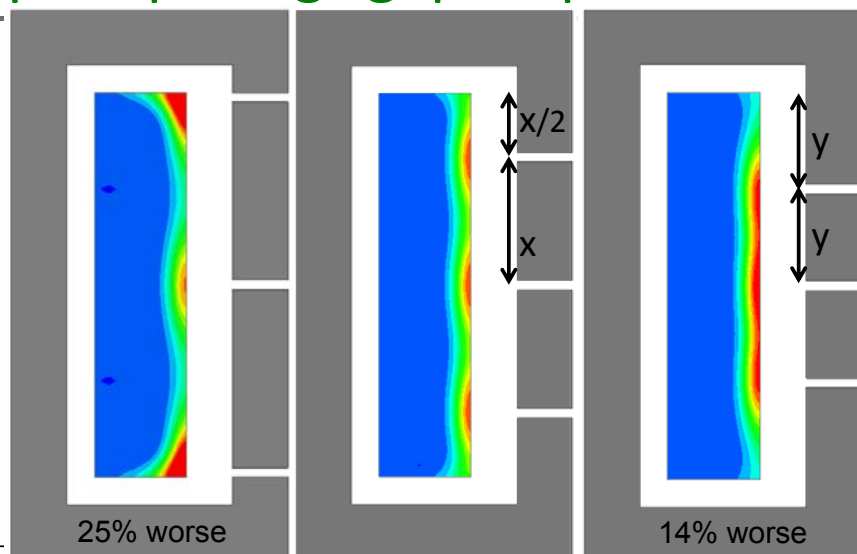


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## Are all equal spacings gaps equal?

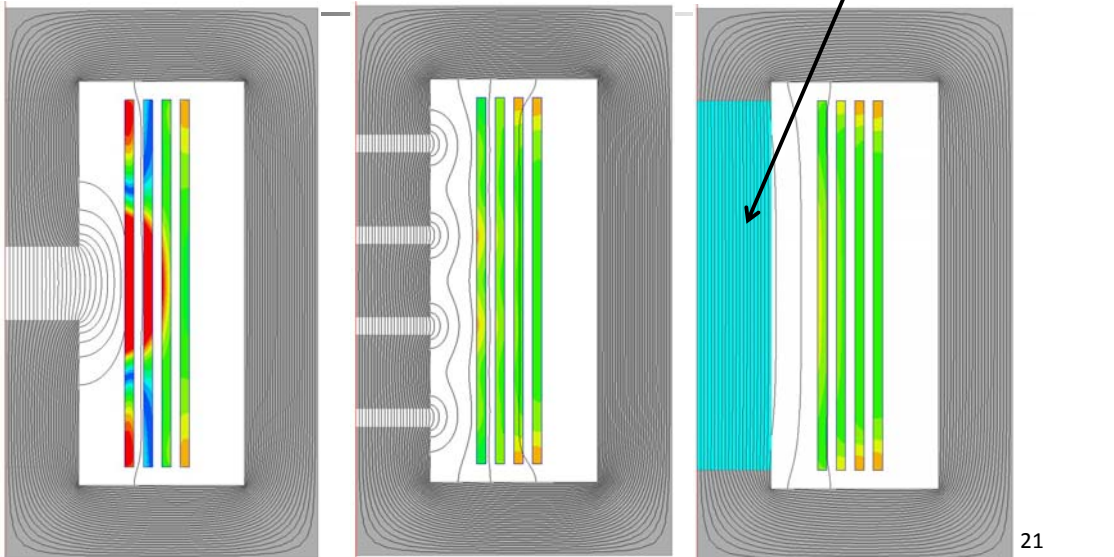
- Current spreads to both sides of gap.
- Position accordingly:  $x/2$  on edges.



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## Approaching distributed gap

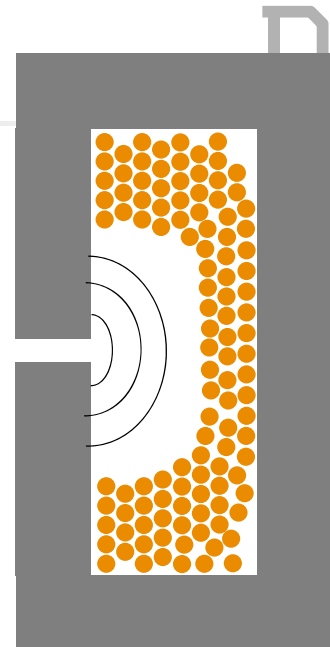


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## Winding shape optimization

- Shape winding configuration to work **with** curved gap field.
- Applies to round wire and litz wire, not foil.
- Can actually work **better** than a distributed gap!
- Ad-hoc approach common, but full optimization is available [2,3,4].

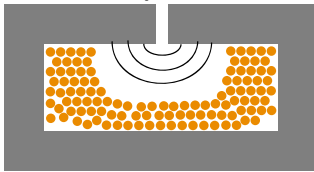


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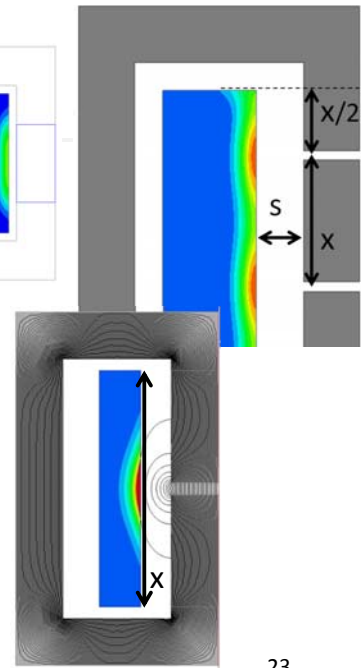
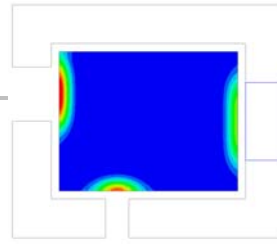
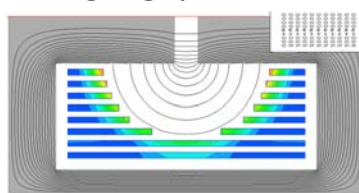


## Fringing conclusions

- Current flows near the gaps.
- A wider gap lowers resistance.
- Spacing  $s > x/3$  is a good rule.
- Not all equally spaced gaps are equal—first gap  $x/2$  from edge.
- Shaped windings with a single gap.



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## Ways forward on core loss: Industry D M

### Magnetic material users

- Ask suppliers for data.
- Estimate skin effect for MnZn ferrites; consider segmented core.
- For non-sinusoidal waveforms: Barg refinement of iGSE (different parameters for each segment).

### Magnetic material suppliers

- Data with dc-bias.
- Data in electronic form.
- Data for different core sizes.
- Data on resistivity (and permittivity?).
- Tolerances: min and max loss
- Data for square-wave drive.

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# Ways forward on core loss: research D

- Integration of models for different loss effects.
  - Hope: effects considered separate maybe different aspects of the same effect.
  - Comprehensive, accurate, research models.
  - Practical, usable models for designers.
- Simple, nonlinear simulation models.
  - Linear models can't match observed behavior.

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## References: Core loss

- [1] Sobhi Barg, K. Ammous, H. Mejbri, and A. Ammous, "An Improved Empirical Formulation for Magnetic Core Losses Estimation Under Nonsinusoidal Induction," *IEEE Trans. Pow. Electr.* 32(3), March 2017
- [2] Benedict Foo, A. Stein, C. Sullivan, "A Step-by-Step Guide to Extracting Winding Resistance from an Impedance Measurement", APEC 2017.
- [3] K. Venkatachalam, C. R. Sullivan, T. Abdallah, and H. Tacca, "Accurate prediction of ferrite core loss with nonsinusoidal waveforms using only Steinmetz parameters," in *IEEE Workshop on Computers in Pow. Electr.*, 2002. <https://engineering.dartmouth.edu/inductor/papers/IGSE.pdf>
- [4] Glenn Skutt, "High-Frequency Dimensional Effects in Ferrite-Core Magnetic Devices," Virginia Tech, PhD thesis 1996. Available for download from Virginia Tech.
- [5] C. A. Baguley, U. K. Madawala, B. Carsten and M. Nymand, "The Impact of Magnetomechanical Effects on Ferrite B-H Loop Shapes," in *IEEE Transactions on Magnetics*, vol. 48, no. 8, pp. 2284-2292, Aug. 2012. doi: 10.1109/TMAG.2012.2191297
- [6] A.P. Van den Bossche, D.M. Van de Sype, V.C. Valchev, "Ferrite Loss Measurement and Models in Half Bridge and Full Bridge Waveforms," *IEEE Power Electronics Specialists Conference*, 2005. doi: 10.1109/PESC.2005.1581834

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## Fringing References



- [1] Jiankun Hu, C. R. Sullivan, "[AC Resistance of Planar Power Inductors and the Quasidistributed Gap Technique](https://engineering.dartmouth.edu/inductor/papers/gdgi.pdf)", *IEEE Tran. on Power Electr.*, 16(4), pp. 558–567, 2001. <https://engineering.dartmouth.edu/inductor/papers/gdgi.pdf>
- [2] Jiankun Hu, C. R. Sullivan, "[Analytical Method for Generalization of Numerically Optimized Inductor Winding Shapes](#)", *IEEE Power Electronics Specialists Conference*, pp. 568–573, June 1999.
- [3] Jiankun Hu, C. R. Sullivan, "[Optimization of Shapes for Round Wire, High Frequency Gapped Inductor Windings](#)", *IEEE Industry Applications Society Annual Meeting*, pp. 907–911, Oct. 1998.
- [4] C. R. Sullivan, J. D. McCurdy, R. A. Jensen, "[Analysis of Minimum Cost in Shape-Optimized Litz-Wire Inductor Windings](#)", *IEEE Power Electronics Specialists Conference*, June 2001.
- [5] J. D. Pollock, C. R. Sullivan, "[Loss Models for Shaped Foil Windings on Low-Permeability Cores](#)", *IEEE Power Electronics Specialists Conference*, pp. 3122–3128, June 2008.
- [6] J. D. Pollock, C. R. Sullivan, "[Modelling Foil Winding Configurations with Low AC and DC Resistance](#)", *IEEE Power Electronics Specialists Conference*, pp. 1507–1512, June 2005.
- [7] J. Pollock, C. R. Sullivan, "[Gapped-Inductor Foil Windings with Low AC and DC Resistance](#)", *IEEE Industry Applications Society Annual Meeting*, pp. 557–663, Oct. 2004.
- [8] Lundquist, Weyman, Vivien Yang, and Carl Castro. "Low AC resistance foil cut inductor." *Energy Conversion Congress and Exposition (ECCE), 2014 IEEE*. IEEE, 2014.
- [9] US Pat. No. 9,123,461B2
- [10] US Pat. No. 8,466,766

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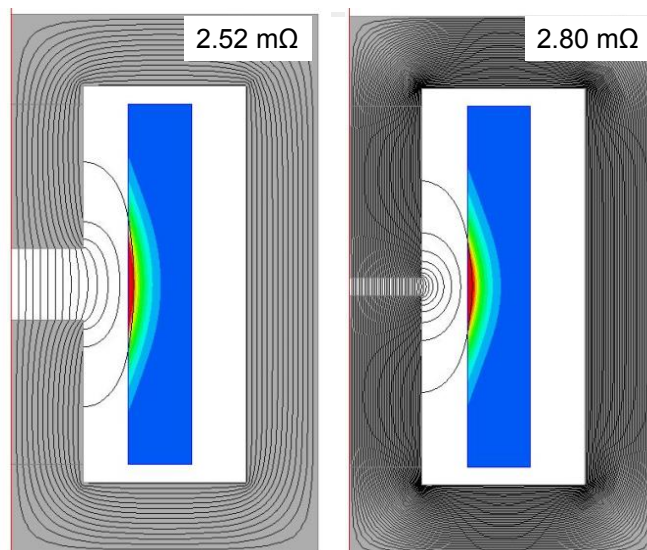
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## Another example



- Both gaps are small enough that it doesn't matter much.
- Shorter gap is worse.



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# Fringing reluctance calculation



$$\mathcal{R}_{faces} = \frac{\pi}{p \cdot \mu_0 \left( 1 + \ln \frac{\pi \ell}{2 \ell_{gap}} \right)}$$
$$\mathcal{R}_{corners} = \frac{1}{\mu_0 k \ell}$$

where

p = perimeter = 2(w+d)

k = 1.23

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